Distribution characteristic and combined optimization of maximum cogging torque of surface mounted few slots permanent-magnet machines

Ping Jin¹, Yujing Guo¹, Jianhu Yan²
¹ School of Energy and Electrical Engineering, Hohai University, Nanjing 211110, P. R. China
² School of Automation, Nanjing University of Science and Technology, Nanjing 210094, P. R. China

This paper examines the maximum cogging torque (MCT) distribution characteristic of surface mounted few slots permanent magnet (SMFSPM) machines. The MCT distributions of SMFSPM machines with different pole-arc coefficients and different ratios of slot opening to slot-pitch are firstly analyzed based on the analytical Fourier series analysis with Maxwell stress tensor method and the finite element method (FEM), respectively. Right triangle distribution regions of the optimal MCT are determined by comparing the MCT distribution contour maps calculated by the two methods. Finally, a combined MCT optimization method for SMFSPM machines is proposed to result in a substantial saving in the optimization time.

Index Terms—maximum cogging torque, few slots permanent magnet machines, right triangle distribution.

I. INTRODUCTION

Surface-mounted few slots permanent magnet (SMFSPM) machines with concentrated windings are attracting the interests of many researchers in recent years because of its short end winding and simple manufacturing process which allows the stator teeth to be manufactured separately to result in a high fill factor in the stator slots [1]-[2]. However, it is noted that improper optimization of the maximum cogging torque (MCT) may lead to serious noise and vibration, thereby undermining the machine’s dynamic performances in a detrimental manner. Although it is feasible to use stator skewing to reduce the MCT, such approach is not very feasible in a high power SMFSPM machine due to its complicated construction. In order to reduce the MCT without skewing the stator, either the pole-arc coefficient or the ratio of slot opening to slot-pitch have been optimized based on numerical and analytical methods. A finite element method (FEM) based on a combination of electromagnetic field and circuit equations for cogging torque prediction is presented [3]. Based on an analytical technique using a relative permeance function, cogging torque can be predicted using either a one-dimensional (1-D) model or a two-dimensional (2-D) model [4]. However, pure analytical method is not accurate enough. Nonetheless, good design results can be obtained by employing the two methods simultaneously.

The purpose of this paper is to examine the MCT distribution characteristic of SMFSPM machines. The MCT distributions of SMFSPM machines with different pole-arc coefficients and ratios of slot opening to slot-pitch are analyzed based on analytical Fourier series analysis with Maxwell stress tensor method and by FEM. Right triangle distribution regions of the optimal MCT are determined by comparing the distribution contour maps obtained by the two methods. A combined MCT optimization method is finally proposed to optimize the MCT of SMFSPM machines with relatively low computer resources.

II. DISTRIBUTION OF MCT

A. Analytical method

Based on the analytical Fourier series analysis with Maxwell stress tensor method, its cogging torque can be expressed as

\[ T = \sum_{k=1}^{N} I_s \int_0^{l_s} \left( \frac{B_{b1}^2 - B_{b2}^2}{2\mu_0} \right) \alpha (\alpha + R_c) d\alpha \]  

where \( R_c \) is the inner radius of stator, \( \delta \) is the ratio of slot opening to slot-pitch, \( l_s \) is the effective axial length of machine, \( B_{b1} \) and \( B_{b2} \) are the two flux densities on the two sides of a tooth, which can also be analytical expressed.

Fig. 1 shows the MCT distribution contour map of the 6/8 SMFSPM machines based on the above analytical formulas, where the maximum MCT is chosen as a reference value and \( R_c, R_m \) and \( R_e \) are constants.

B. Numerical method

Fig. 2 shows the MCT distribution contour map of the typical 6/8 SMFSPM machine based on FEM. The hollow circular points in the contour map denote the optimal points. Comparing with the contour map as shown in Fig. 1, the optimal points seem to be rather randomly distributed. It can
be observed that the optimal $\delta_s$ values are not dependent on $\delta_p$; Neither is the optimal $\delta_p$ values dependent on $\delta_s$. However, when the optimal lines obtained by the analytical method and the optimal points obtained by the FEM are overlapped in one figure, the distribution of the optimal points looks more orderly.

2) determine the right-angled triangles containing the optimal points;
3) search for the optimal points in the right-angled triangles using FEM.

As there exists only two or three optimal points in each right-angled triangle, a local optimal algorithm, such as coarse and fine meshes, can be applied for searching for the optimal points. Table I gives a comparison of the optimal results and costing times with different methods when $\delta_s \in (0.5, 0.75)$ and $\delta_p \in (0.5, 0.75)$. The values of $\delta_s$ and $\delta_p$ are obtained by the analytical Fourier series analysis with Maxwell stress tensor method, FEM, the combined method, and the combined method with coarse and fine meshes respectively. The entries of Table I show that the combined method has a relatively high efficiency. Fig. 5 gives the cogging torque results of the 6/8 SMFSPM machine with optimal $\delta_s$ and $\delta_p$ obtained by the proposed methods.

<table>
<thead>
<tr>
<th>Methods</th>
<th>Optimal results ($\delta_s$,$\delta_p$)</th>
<th>Times</th>
</tr>
</thead>
<tbody>
<tr>
<td>Analytical analysis</td>
<td>0.8739Nm (0.65, 0.75)</td>
<td>2 min</td>
</tr>
<tr>
<td>FEM</td>
<td>0.2843 Nm (0.68, 0.54)</td>
<td>31 hours</td>
</tr>
<tr>
<td>Combined method</td>
<td>0.2488 Nm (0.67, 0.56)</td>
<td>8 hours</td>
</tr>
<tr>
<td>Combined method with course and fine meshes *</td>
<td>0.1811 Nm (0.62, 0.69)</td>
<td>1.5 hours</td>
</tr>
</tbody>
</table>

* the size of coarse meshes is 0.03; the size of fine meshes is 0.01.

ACKNOWLEDGMENT

This work was jointly supported by the NSFC (51407061) and the NSF of Jiangsu Province (BK20140854).

REFERENCES